

$$\vec{A} = \vec{A}_x + \vec{A}_y$$

$$A_x = A \cos \theta \quad \theta = \tan^{-1} \left(\frac{A_y}{A_x} \right)$$

$$A_y = A \sin \theta$$

$$A = \sqrt{A_x^2 + A_y^2} \quad \tan \theta = \frac{A_y}{A_x}$$

$$v_{avg} = \frac{\Delta x}{\Delta t} = \frac{x_f - x_i}{t_f - t_i}$$

$$v_{inst} \equiv \lim_{\Delta t \rightarrow 0} \frac{\Delta x}{\Delta t}$$

$$a_{avg} = \frac{\Delta v}{\Delta t} = \frac{v_f - v_i}{t_f - t_i}$$

$$a_{inst} \equiv \lim_{\Delta t \rightarrow 0} \frac{\Delta v}{\Delta t}$$

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$$\Delta x = v_0 t + \frac{1}{2} a t^2$$

$$\Delta x = \frac{1}{2} (v_0 + v) t$$

$$v = v_0 + a t$$

$$v^2 = v_0^2 + 2 a \Delta x$$

$$\Delta \vec{r} = \vec{r}_f - \vec{r}_i$$

$$\vec{v}_{avg} = \frac{\Delta \vec{r}}{\Delta t}$$

$$\vec{v}_{inst} \equiv \lim_{\Delta t \rightarrow 0} \frac{\Delta \vec{r}}{\Delta t}$$

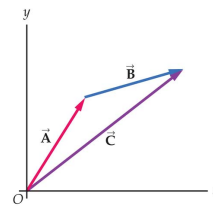
$$\vec{a}_{avg} = \frac{\Delta \vec{v}}{\Delta t}$$

$$\vec{a}_{inst} \equiv \lim_{\Delta t \rightarrow 0} \frac{\Delta \vec{v}}{\Delta t}$$

$$\vec{C} = \vec{A} + \vec{B}$$

$$C_x = A_x + B_x$$

$$C_y = A_y + B_y$$



$$v_x = v_{0x} + a_x t \quad v_y = v_{0y} + a_y t$$

$$\Delta x = v_{0x} t + \frac{1}{2} a_x t^2 \quad \Delta y = v_{0y} t + \frac{1}{2} a_y t^2$$

$$v_x^2 = v_{0x}^2 + 2 a_x \Delta x \quad v_y^2 = v_{0y}^2 + 2 a_y \Delta y$$

projectile motion

$$v_y = v_0 \sin \theta_0 - g t$$

$$v_x = v_{0x} = v_0 \cos \theta_0 \quad \Delta y = v_0 \sin \theta_0 t - \frac{1}{2} g t^2$$

$$\Delta x = v_{0x} t \quad R = \sin(2\theta_0) v_0^2 / g$$

$$A t^2 + B t + C = 0; \quad t = \frac{-B \pm \sqrt{B^2 - 4AC}}{2A}$$

$$g = 9.80 \text{ m/s}^2 \text{ down} \quad \vec{V}_{AB} = \vec{V}_{AC} + \vec{V}_{CB}$$

$$\vec{a} = \frac{\Sigma \vec{F}}{m}; \quad \Sigma \vec{F} = m \vec{a}; \quad \vec{F}_{12} = -\vec{F}_{21}; \quad \text{weight } W = mg; \quad f_k = \mu_k n; \quad f_s^{\max} = \mu_s n; \quad F_D = \frac{1}{2} C \rho A v^2;$$

$$v_t = \sqrt{2mg / (C \rho A)}; \quad \rho_{air} = 1.21 \text{ kg/m}^3; \quad W = (F \cos \theta) d; \quad K = \frac{1}{2} m v^2; \quad W_{total} = \frac{1}{2} m v_f^2 - \frac{1}{2} m v_0^2; \quad U_g = mgy;$$

$$F_s = -kx; \quad U_s = \frac{1}{2} k x^2; \quad \text{mech. energy } E = U + K; \quad W_c = U_i - U_f; \quad W_{nc} = E_f - E_0; \quad W_{total} = W_c + W_{nc};$$

$$\vec{P} = \frac{W}{t} = F \vec{v}; \quad \text{centrip. } a_{CP} = v^2 / R; \quad f_{CP} = m v^2 / R; \quad \text{stress} = \text{modulus} * \text{strain, e.g. } F / A = Y(\Delta L / L_0)$$

impulse $\vec{I} = \vec{F}_{av} \Delta t = \Delta \vec{p}; \quad \vec{p} = m \vec{v}; \quad p_x = m v_x; \quad p_y = m v_y; \quad \vec{F} = \Delta \vec{p} / \Delta t; \quad \Sigma \vec{p} = \text{const. when } \Sigma \vec{F}_{ext} = 0;$

perfect inelas. coll. $\Rightarrow \vec{v}_f = \frac{m_1 \vec{v}_{01} + m_2 \vec{v}_{02}}{m_1 + m_2};$ *elastic 1D* $\Rightarrow v_{1f} = \frac{m_1 - m_2}{m_1 + m_2} v_{1i}; \quad v_{2f} = \frac{2m_1}{m_1 + m_2} v_{1i};$
(stuck - together) m_2 initially as rest

$$x_{CM} = \frac{\Sigma m_i x_i}{\Sigma m_i}; \quad y_{CM} = \frac{\Sigma m_i y_i}{\Sigma m_i}; \quad \vec{v}_{CM} = \frac{\Sigma m_i \vec{v}_i}{\Sigma m_i}; \quad \vec{a}_{CM} = \frac{\Sigma m_i \vec{a}_i}{\Sigma m_i} = \frac{\Sigma \vec{F}_{ext}}{M}; \quad \text{thrust} = \left| v_e \frac{\Delta M}{\Delta t} \right|;$$

$$\theta (\text{in radians}) = \frac{s}{r}; \quad \omega_{av} = \frac{\Delta \theta}{\Delta t} = \frac{\theta - \theta_0}{t - t_0}; \quad \alpha_{av} = \frac{\Delta \omega}{\Delta t} = \frac{\omega - \omega_0}{t - t_0}; \quad \omega = \lim_{\Delta t \rightarrow 0} \frac{\Delta \theta}{\Delta t}; \quad \alpha = \lim_{\Delta t \rightarrow 0} \frac{\Delta \omega}{\Delta t};$$

$$v_t = r \omega; \quad a_t = r \alpha; \quad \theta = \omega_0 t + \frac{1}{2} \alpha t^2; \quad \theta = \frac{1}{2} (\omega_0 + \omega) t; \quad \omega = \omega_0 + \alpha t; \quad \omega^2 = \omega_0^2 + 2 \alpha \theta; \quad a = \sqrt{a_c^2 + a_t^2};$$

$$a_c = v^2 / r = \omega^2 r; \quad F_c = m v^2 / r; \quad \tau = r F \sin \theta; \quad \tau = m r^2 \alpha; \quad \Sigma \tau = \Delta L / \Delta t = I \alpha; \quad I = \Sigma m r^2;$$

$$W_R = \tau \theta; \quad K_R = \frac{1}{2} I \omega^2; \quad L_i = L_f; \quad L = I \omega; \quad \vec{L} = \vec{r} \times \vec{p} = l p = m r v \sin \theta; \quad \text{equilib. } \Rightarrow \Sigma \vec{F} = 0 \text{ and } \Sigma \vec{\tau} = 0;$$

$$I = MR^2 \text{ thin cylindrical shell}; \quad I = \frac{1}{2} MR^2 \text{ solid disk}; \quad I = \frac{2}{3} MR^2 \text{ thin spherical shell}; \quad I = \frac{2}{5} MR^2 \text{ solid sphere}; \quad E = \frac{1}{2} I \omega^2 + \frac{1}{2} m v^2 + \frac{1}{2} k x^2 + mgy$$

$$F_G = \frac{-GMm}{r^2}; G=6.67 \times 10^{-11} \text{ N m}^2 \text{ kg}^{-2}; R_E=6.38 \times 10^6 \text{ m}; M_E=5.98 \times 10^{24} \text{ kg}; g = \frac{GM_E}{R_E^2}; U = \frac{-GM_E m}{r};$$

$$\text{orbit } v = \sqrt{\frac{GM_S}{r}}; T = \frac{2\pi r^{3/2}}{\sqrt{GM_S}}; \text{Kepler: } T^2 = \left(\frac{4\pi^2}{GM_S}\right)r^3; v_{esc} = \sqrt{\frac{2GM_E}{R_E}};$$

$$\text{SHM } 2\pi f = \omega = \sqrt{\frac{k}{m}}; T = \frac{2\pi}{\omega} = 2\pi \sqrt{\frac{m}{k}}; f = \frac{1}{T} = \frac{1}{2\pi} \sqrt{\frac{k}{m}}; x = A \cos(\omega t + \theta_0); v = -A\omega \sin(\omega t + \theta_0); a = -A\omega^2 \cos(\omega t + \theta_0);$$

$$v_{\max} = A\omega; a_{\max} = A\omega^2 = kA/m; E_{total} = \frac{1}{2}kA^2; v = \pm \sqrt{\frac{k}{m}(A^2 - x^2)}; \text{pend. } \omega = \sqrt{\frac{g}{L}}; T = 2\pi \sqrt{\frac{L}{g}}; T = 2\pi \sqrt{\frac{I}{mgl}};$$

$$\text{damp } f_F = -bv; x = A_0 e^{-bt/2m} \cos(\omega_0 t + \theta_0); \text{crit.damp } b/(2m) = \omega_0 = \sqrt{k/m}; \omega_{res}^2 = \omega_0^2 - b^2/(2m^2)$$

$$v = \frac{\lambda}{T} = \lambda f; v = \sqrt{\frac{F}{m/L}}; y(x,t) = A \cos\left(\frac{2\pi x}{\lambda} - \frac{2\pi t}{T}\right); v = 343 \text{ m/s}; I = \frac{P}{A}; I = \frac{P}{4\pi r^2}; \frac{I_1}{I_2} = \frac{r_2^2}{r_1^2};$$

$$\beta = 10 \text{ dB} \times \log\left(\frac{I}{I_0}\right); I = I_0 \cdot 10^{\beta/10}; I_0 = 1.0 \times 10^{-12} \text{ W/m}^2; f_o = f_s \left(\frac{v \pm v_o}{v \mp v_s}\right); r_2 - r_1 = n\lambda \text{ construc.};$$

$$r_2 - r_1 = (n + \frac{1}{2})\lambda \text{ destruct.}; \text{stand.wave.string } f_1 = v/(2L); f_2 = 2f_1, f_3 = 3f_1;$$

$$f_n = nf_1 = \frac{nv}{2L}, n=1,2,3,\dots \text{ open both ends}; f_n = \frac{nv}{4L}, n=1,3,5,\dots \text{ open one end}; f_{beat} = |f_1 - f_2|;$$

$$\rho = M/V; \rho = (\text{Specific Gravity}) \cdot \rho_{water}; \rho_{water} = 1000 \text{ kg/m}^3; P = F/A; Pa = N/m^2; P = P_{at} + \rho gh;$$

$$P_{at} = 1.01 \times 10^5 \text{ Pa}; P_{gauge} = P - P_{at}; \text{buoyant } F_b = \rho_{fluid} V_{displaced} g; \rho_1 v_1 A_1 = \rho_2 v_2 A_2; \text{Bernoulli}$$

$$P + \frac{1}{2}\rho v^2 + \rho gh = \text{const.}; v = \sqrt{2gh}; P_1 - P_2 = 8\pi\eta v L/A; dV/dt = (P_1 - P_2)\pi r^4/(8\eta L)$$

$$T_C = T - 273.15; T_F = \frac{9}{5}T_C + 32; T_C = \frac{5}{9}(T_F - 32); \Delta L = \alpha L_0 \Delta T; L - L_0 = \alpha L_0 (T - T_0); \Delta V = \beta V_0 \Delta T;$$

$$V = V_0 + \beta V_0 (T - T_0); \beta = 3\alpha; 1 \text{ cal} = 4.186 \text{ J}; \text{heat cap. } C \equiv \frac{Q}{\Delta T}; \text{spec. heat } c \equiv \frac{Q}{m\Delta T}; Q = kA \frac{\Delta T}{L} t;$$

$$P = \sigma A e T^4; \phi_{net} = \sigma A e (T^4 - T_0^4);$$

$$PV = nRT = Nk_B T; N_A = 6.02 \times 10^{23} \text{ part./mole}; R = 8.31 \text{ J/mol} \cdot \text{K}; k_B = R/N_A = 1.38 \times 10^{-23} \text{ J/K};$$

$$\frac{1}{2}mv^2 = \frac{3}{2}k_B T; U = \frac{3}{2}nRT; v_{rms} = \sqrt{v^2} = \sqrt{\frac{3k_B T}{m}} = \sqrt{\frac{3RT}{M}}; W = -P\Delta V; C_v = \frac{3}{2}R; \Delta U = nC_v \Delta T; \text{adiab.}$$

$$PV^\gamma = \text{const.}; \text{latent heat } Q \equiv \pm mL; \gamma = C_p/C_v; W_{env} = nRT \ln(V_f/V_i); W_{env} = |Q_h| - |Q_c|;$$

$$e = \frac{W_{env}}{|Q_h|} = \frac{|Q_h| - |Q_c|}{|Q_h|} = 1 - \frac{|Q_c|}{|Q_h|}; \frac{|Q_c|}{|Q_h|} = \frac{T_c}{T_h}; e_c = 1 - \frac{T_c}{T_h}; \Delta S \equiv \frac{Q_r}{T}; S = k_B \ln W;$$

